

Use proper mathematical notation at all times.

1. A surface is given by $z = x^3 + x^2y + xy^2 + y^3$. Determine
 - (a) $z_x(-1, 2)$
 - (b) $z_y(-1, 2)$
 and then answer the following.
 - i. State the slope of the tangent line to the surface at point $(-1, 2, 5)$ in the plane parallel to the yz -plane.
 - ii. State the slope of the tangent line to the surface at point $(-1, 2, 5)$ in the plane parallel to the xz -plane.
 - iii. At what rate is z changing at point $(-1, 2, 5)$ in the plane $y = 2$?
 - iv. At what rate is z changing at point $(-1, 2, 5)$ in the plane $x = -1$?

2. For each of the following functions, determine (i) $\frac{\partial f}{\partial x}$ and (ii) $\frac{\partial f}{\partial y}$.
 - (a) $f(x, y) = x^2 \cos y^3$
 - (b) $f(x, y) = \sin(x^2 y^3)$
 - (c) $f(x, y) = e^{x^2 y^4}$
 - (d) $f(x, y) = e^{x^2 + y^4}$
 - (e) $f(x, y) = e^{x^2 + y^4} \tan y^3$
 - (f) $f(x, y) = e^{x^2} \cot(x^2 y^3)$
 - (g) $f(x, y) = \ln(x^2 y^4)$
 - (h) $f(x, y) = \frac{xy}{x + y}$

NOTE: In Maple, partial differentiation is no different from differentiation. Use Maple to check your answers to the above. For example,

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> f := x^2 * cos(y^3); <ret>                                     defines f as an expression

> diff(f,x); <ret>                                               gives  $\frac{\partial f}{\partial x}$ 

> diff(f,y); <ret>                                               gives  $\frac{\partial f}{\partial y}$ 

> diff(f,x,y); <ret>                                             gives  $\frac{\partial^2 f}{\partial y \partial x}$ 

> diff(f,x$2); <ret>                                             gives  $\frac{\partial^2 f}{\partial x^2}$ 

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